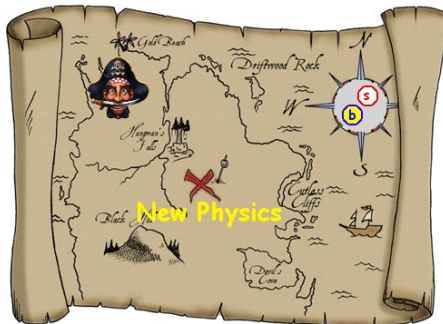
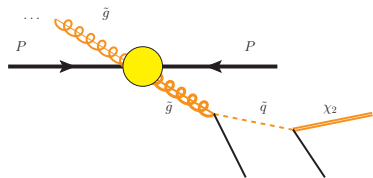


Lessons from B_s Lifetimes

Rob Knegjens

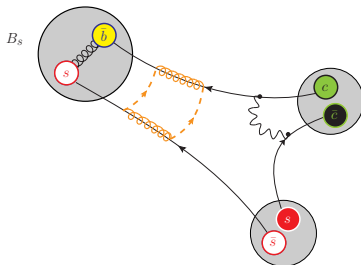


The search for **New Physics**

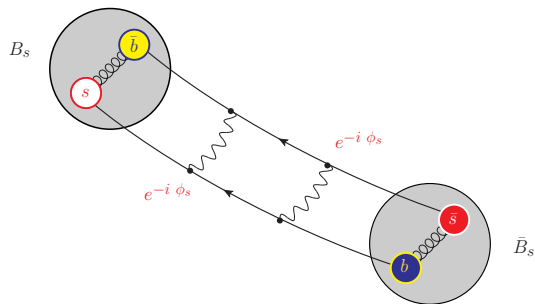


Direct searches
"The high energy frontier"

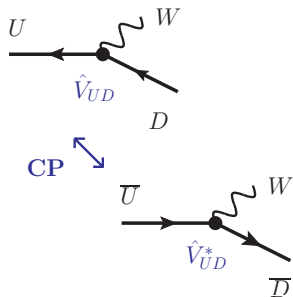
Indirect searches
"The precision frontier"



A sensitive probe of **New CP Violating Physics**



Standard Model:



$$2 \arg(V_{ts} V_{tb}^*) = -2.1^\circ$$

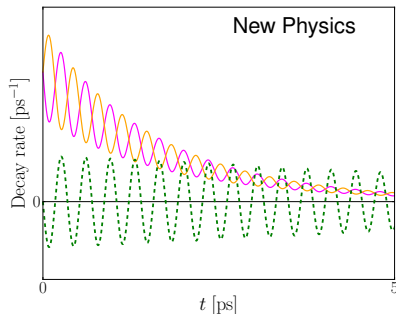
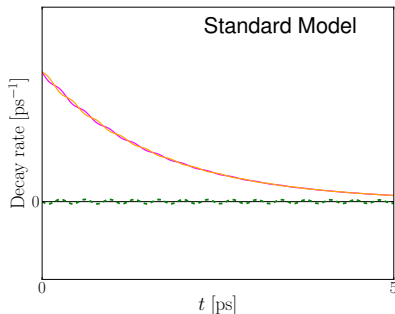
$B_s - \bar{B}_s$ **Mixing Phase:**

$$\phi_s \equiv -2.1^\circ + \text{treasure chest icon}$$

Time-dependent **tagged** CP measurement

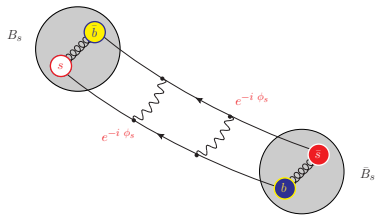
Tag \equiv identify if B_s or \bar{B}_s

$$A_{\text{CP}} = \frac{\Gamma(B_s(t) \rightarrow f) - \Gamma(\bar{B}_s(t) \rightarrow f)}{\Gamma(B_s(t) \rightarrow f) + \Gamma(\bar{B}_s(t) \rightarrow f)}$$



CP violation in interference

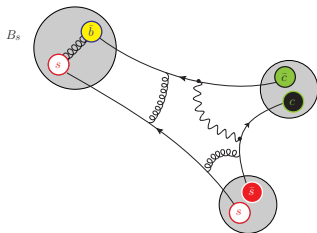
$B_s^0 - \bar{B}_s^0$ Mixing



$$\Delta M_s, \Delta \Gamma_s \equiv \Gamma_L - \Gamma_H$$

$$\left. \begin{array}{l} \phi_s \end{array} \right\} \text{ } \img alt="Treasure chest icon" data-bbox="298 648 371 742"/>$$

Decay Mode



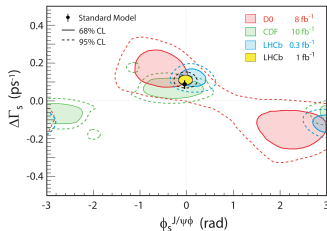
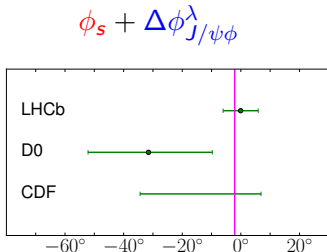
$$\Delta \phi, C \text{ (direct CPV)}$$

$$\left. \begin{array}{l} \text{hadronic physics} \end{array} \right\} \text{ } \img alt="Question mark icon" data-bbox="812 658 858 738"/> \img alt="Cartoon character icon" data-bbox="875 645 951 748"/>$$

$$A_{CP} = \text{function} \left(\Delta M_s, \Delta \Gamma_s, \boxed{\phi_s + \Delta \phi}, C \right)$$

The flagship Decay Mode: $B_s \rightarrow J/\psi \phi$

Latest results from Moriond 2012:

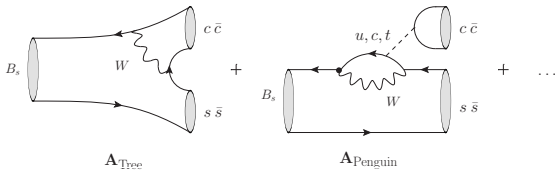


CP observables \rightarrow SM predictions

- Possible to distinguish smallish New Physics?

$$\Delta\phi = ??$$

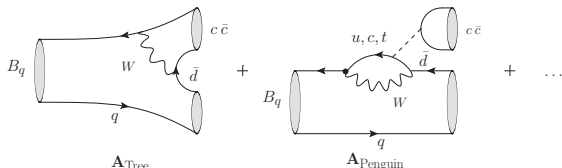
Optimal **Decay Mode** structure: $B_s \rightarrow \underbrace{J/\psi}_{\bar{c}c} \underbrace{\phi}_{\bar{s}s}$



$$\begin{aligned}
 A(B_s \rightarrow \bar{c}c\bar{s}s) &= A_T V_{cb}^* V_{cs} + A_P^u V_{ub}^* V_{us} + A_P^c V_{cb}^* V_{cs} + A_P^t V_{tb}^* V_{ts} + \dots \\
 &= \mathcal{A} \left[1 + \underbrace{\lambda^2}_{0.05} e^{i\gamma} b e^{i\theta} \right], \quad \text{in SM : } \gamma \sim 70^\circ
 \end{aligned}$$

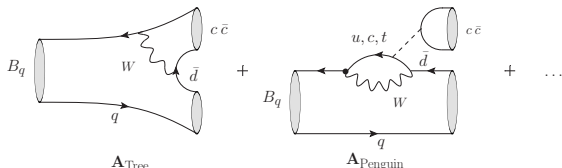
$$\boxed{b e^{i\theta} = \underbrace{\left(\frac{1}{\lambda} - \frac{\lambda}{2}\right)}_{\sim \frac{1}{2}} \left| \frac{V_{ub}}{V_{cb}} \right| \left(\frac{A_P^{(ut)}}{A_T + A_P^{(ct)}} \right)} \quad \left\{ \begin{array}{l} C = - \overbrace{\lambda^2}^{5\%} \sin \gamma \, 2b \sin \theta + \mathcal{O}(\epsilon^2) \\ \Delta\phi = \underbrace{\lambda^2}_{3^\circ} \sin \gamma \, 2b \cos \theta + \mathcal{O}(\epsilon^2) \end{array} \right.$$

Penguin control via flavour symmetry



$$A(B_q \rightarrow \bar{c}c\bar{d}q) \stackrel{SU(3)_F}{=} -\lambda \mathcal{A} \left[1 - \underbrace{\cancel{1}}_1 e^{i\gamma} b e^{i\theta} \right]$$

Penguin control via flavour symmetry



$$A(B_q \rightarrow \bar{c}c\bar{d}q) \stackrel{SU(3)_F}{=} -\lambda \mathcal{A} \left[1 - \underbrace{\lambda^2}_1 e^{i\gamma} b e^{i\theta} \right]$$

- Example: $B_d \rightarrow J/\psi K^0$ to $B_d \rightarrow J/\psi \pi^0$:

$$b \in [0.15, 0.67], \quad \theta \in [174^\circ, 212^\circ] \quad \implies \quad \Delta\phi_{J/\psi K^0}^d = [-3.9^\circ, -0.8^\circ]$$

S. Faller, R. Fleischer, M. Jung, T. Mannel, PRD 79 014030 (2009) M.

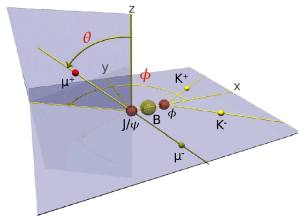
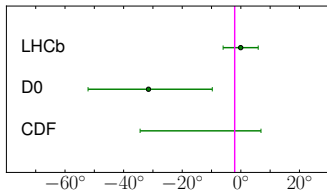
Ciuchini, M. Pierini, L. Silvestrini, PRL 95 221804 (2005)/arXiv:1102.0392

- Soon also $B_s \rightarrow J/\psi K^0$

K. De Bruyn, R. Fleischer, P. Koppenburg, Eur.Phys.J. C70 (2010) 1025-1035

The flagship Decay Mode: $B_s \rightarrow J/\psi \phi$

$$\phi_s + \overbrace{\Delta\phi_{J/\psi\phi}^\lambda}^{[-3^\circ, 3^\circ]}$$



- Future control channels: $B_s \rightarrow J/\psi \bar{K}^{*0}$ and $B_d \rightarrow J/\psi \rho^0$

S. Faller, R. Fleischer and T. Mannel, Phys.Rev. D79 (2009) 014005



CP observables \rightarrow SM predictions

Disentangle **New Physics** 

from **SM Hadronic Physics** 

and

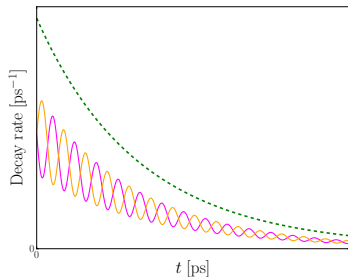


Find **Complementary Analyses**
for determining ϕ_s

- **In pursuit of new physics with $B_s \rightarrow K^+ K^-$** R. Fleischer, RK (arXiv:1011.1096)
- **Anatomy of $B_{s,d}^0 \rightarrow J/\psi f_0(980)$** R. Fleischer, RK, G. Ricciardi (arXiv:1109.1112)
- **Effective lifetimes of B_s decays and their constraints on the $B_s^0-\bar{B}_s^0$ mixing parameters** R. Fleischer, RK (arXiv:1109.5115)
- **Exploring CP Violation and $\eta-\eta'$ Mixing with the $B_{s,d}^0 \rightarrow J/\psi\eta^{(\prime)}$ Systems**
R. Fleischer, RK, G. Ricciardi (arXiv:1110.5490)

A time-dependent **untagged** analysis?

$$\langle \Gamma_f \rangle \equiv \Gamma(B_s(t) \rightarrow f) + \Gamma(\bar{B}_s(t) \rightarrow f)$$

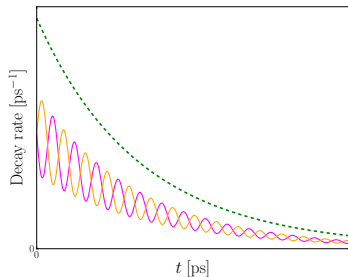


A time-dependent **untagged** analysis?

$$\langle \Gamma_f \rangle \equiv \Gamma(B_s(t) \rightarrow f) + \Gamma(\bar{B}_s(t) \rightarrow f)$$

$$\propto e^{-\Gamma_s t} \left[\cosh(\Delta\Gamma_s t) + \underbrace{\mathcal{A}_{\Delta\Gamma}^f}_{\text{function}(\phi_s + \Delta\phi_f, C_f)} \sinh(\Delta\Gamma_s t) \right]$$

$$\Delta\Gamma_s \equiv \Gamma_L - \Gamma_H$$



Fitting $\frac{1}{\tau} e^{-t/\tau}$ - **effective lifetime:**

$$\tau_f \equiv \frac{\int_0^\infty t \langle \Gamma_f \rangle dt}{\int_0^\infty \langle \Gamma_f \rangle dt}$$

$$= \text{function}(\Delta\Gamma_s, \underbrace{\phi_s}_{\text{treasure chest}} + \Delta\phi_f, C_f)$$



Contours in the $\phi_s - \Delta\Gamma_s$ plane

$$\tau_f = \frac{\tau_{B_s}}{1 - y_s^2} \left(\frac{1 + 2\mathcal{A}_{\Delta\Gamma}^f y_s + y_s^2}{1 + \mathcal{A}_{\Delta\Gamma}^f y_s} \right), \quad y_s \equiv \Delta\Gamma_s / 2\Gamma_s$$

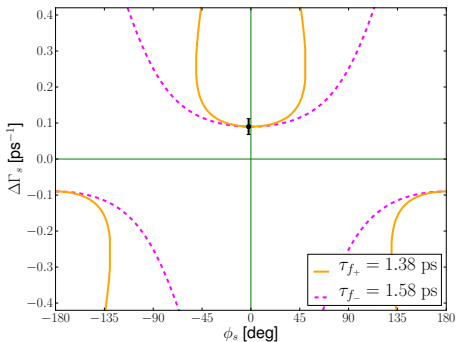
$$\mathcal{A}_{\Delta\Gamma}^f = -\eta_f \sqrt{1 - C_f^2} \cos(\phi_s + \Delta\phi_f)$$

$$\mathcal{CP}|f\rangle = \eta_f |f\rangle$$

Assuming:

$$\Delta\phi_f = 0, \quad C_f = 0$$

$$\mathcal{A}_{\Delta\Gamma}^f = \begin{cases} -\cos\phi_s & : f_{\text{even}} \\ +\cos\phi_s & : f_{\text{odd}} \end{cases}$$



Measured Effective Lifetimes

Final state:

- **CP Even** $B_s \rightarrow K^+ K^-$: *LHCB, arXiv:1207.5993*

$$\tau_{K^+ K^-} = [1.455 \pm 0.046 \pm 0.006] \text{ ps}$$

- **CP Odd** $B_s \rightarrow J/\psi f_0(980)$: *LHCb, arXiv:1207.0878*

$$\tau_{J/\psi f_0} = [1.700 \pm 0.040 \pm 0.026] \text{ ps}$$

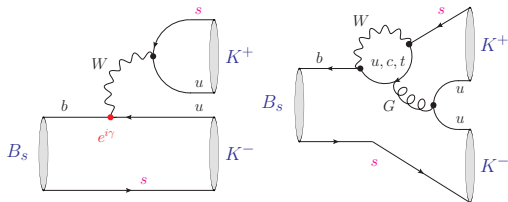
But...

$$\Delta\phi \neq 0, \quad C \neq 0$$

... CP violation in **Decay Modes**

Controlling the **CP Even** Decay Mode

$$B_s \rightarrow K^+ K^-$$



$$\Delta\phi_{K^+K^-} = - (10.5^{+3.1}_{-2.8})^\circ$$

$$C_{K^+K^-} = 0.09 \pm 0.05$$

- Use ***U-spin* flavour symmetry** (subgroup $SU(3)_F$):

interchange $s \leftrightarrow d$ quarks

Related to $B_d \rightarrow \pi^+ \pi^-$

Extract **CP violating phase**: $\gamma = (68 \pm 7)^\circ$

R. Fleischer and RK, Eur.Phys.J. C71 (2011) 1532

Controlling the **CP Odd** Decay Mode

S. Stone and L. Zhang, *Phys. Rev. D* 79 (2009)

$$B_s / \bar{B}_s \rightarrow J/\psi \phi \not\propto f_0(980)$$

$f_0(980)$ [a]

$I^G(J^{PC}) = 0^+(0^{++})$

$f_0(980)$ Section References

See also the [minireview on scalar mesons](#) .

Mass $m = (980 \pm 10)$ MeV

Full width $\Gamma = 40$ to 100 MeV

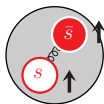
$f_0(980)$ DECAY MODES

Γ_i	Mode	Fraction (Γ_i / Γ)	p (MeV/c)
Γ_1	$\pi\pi$	dominant	471
Γ_2	$K\bar{K}$	seen	-1
Γ_3	$\gamma\gamma$	seen	490
Γ_4	e^+e^-		490

Controlling the **CP Odd** Decay Mode

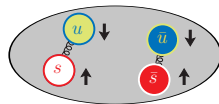
$$B_s \rightarrow J/\psi f_0(980)$$

Quark-antiquark



What is
 $f_0(980)$?

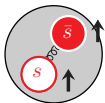
Tetraquark



Controlling the CP Odd Decay Mode

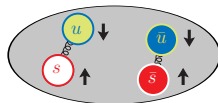
$$B_s \rightarrow J/\psi f_0(980)$$

Quark-antiquark

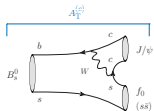


What is $f_0(980)$?

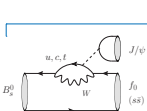
Tetraquark



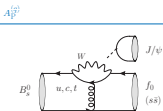
- Decay amplitudes may vary:



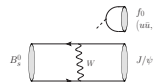
Colour-suppressed Tree



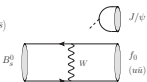
Penguin



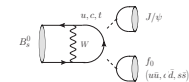
Penguin Exchange



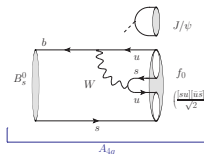
Exchange



Exchange



Penguin Annihilation



A_{4q}

Controlling the **CP Odd** Decay Mode

- Propose **control channel**: $B_d \rightarrow J/\psi f_0(980)$
- **Useful** if :

$$A_T, A_P \gg A_E, A_{PA}, A_{4q}$$

- With SM CP violation and **unknown decay amplitudes**:

$$\Delta\phi_{J/\psi f_0} \in [-3^\circ, 3^\circ], \quad C_{J/\psi f_0} \lesssim 0.05$$

- **Predict**:

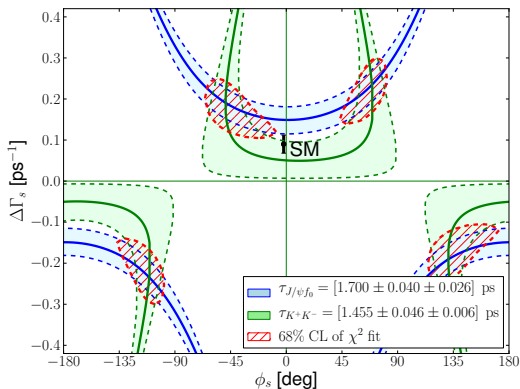
$$\begin{aligned} & \text{BR}(B_d \rightarrow J/\psi f_0; f_0 \rightarrow \pi^+ \pi^-) \\ & \sim (1 - 3) \times 10^{-6} \times \begin{cases} \left[\frac{\tan \varphi_M}{\tan 35^\circ} \right]^2 & : \quad q\bar{q} \\ 1 & : \quad \text{tetraquark} \end{cases} \end{aligned}$$

R. Fleischer, RK, G. Ricciardi, Eur.Phys.J. C71 (2011) 1832

Lifetime contours in the $\phi_s - \Delta\Gamma_s$ plane

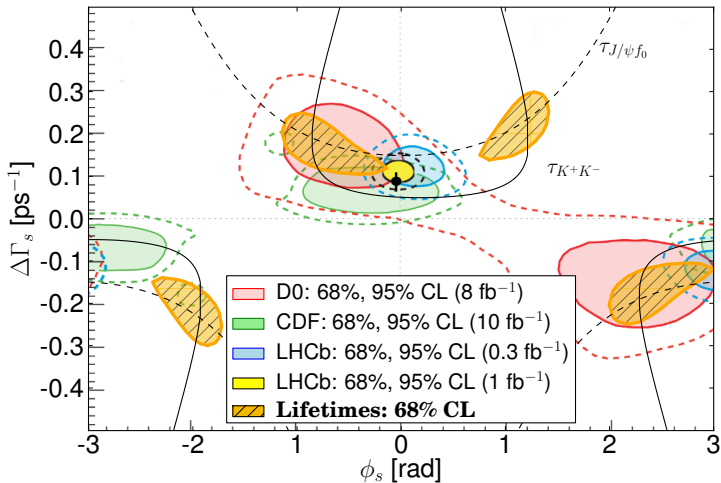
$$\tau_f = \text{function} \left(\Delta\Gamma_s, \boxed{\phi_s + \Delta\phi}, C \right)$$

- **CP Even** : τ_{K+K^-} , $\Delta\phi_{K+K^-} = -(10.5^{+3.1}_{-2.8})^\circ$, $C_{K+K^-} = 0.09$
- **CP Odd** : $\tau_{J/\psi f_0}$, $\Delta\phi_{J/\psi f_0} \in [-3^\circ, 3^\circ]$, $C_{J/\psi f_0} \leq 0.05$



R. Fleischer and RK, Eur.Phys.J. C71 (2011) 1532

Untagged determination of B_s mixing parameters



B_s Branching Ratios

K. Bruyn, R. Fleischer, RK, P. Koppenburg, M. Merk, N. Tuning, Phys.Rev.D 86 (2012)

- Measured:

$$\begin{aligned}\text{BR}(B_s \rightarrow f)_{\text{exp}} &\equiv \frac{1}{2} \int_0^{\infty} \langle \Gamma_f(t) \rangle dt \\ &= \frac{1}{2} \left[\frac{\Gamma(B_H \rightarrow f)}{\Gamma_H} + \frac{\Gamma(B_L \rightarrow f)}{\Gamma_L} \right]\end{aligned}$$

- Computed:

$$\begin{aligned}\text{BR}(B_s \rightarrow f)_{\text{theo}} &\equiv \frac{1}{2} \left[\frac{\Gamma(B^0 \rightarrow f) + \Gamma(\bar{B}^0 \rightarrow f)}{\frac{1}{2}(\Gamma_H + \Gamma_L)} \right] \\ &= \frac{1}{2} \left[\frac{\Gamma(B_H \rightarrow f) + \Gamma(B_L \rightarrow f)}{\frac{1}{2}(\Gamma_H + \Gamma_L)} \right]\end{aligned}$$

- Dictionary for $\Delta\Gamma_s \equiv \Gamma_L - \Gamma_H \neq 0$ via effective lifetime τ_f :

$$\text{BR}(B_s \rightarrow f)_{\text{theo}} = \left[2 - (1 - y_s^2) \frac{\tau_f}{\tau_{B_s}} \right] \text{BR}(B_s \rightarrow f)_{\text{exp}}$$

Probing New Physics in $B_s \rightarrow \mu^+ \mu^-$

K. Bruyn, R. Fleischer, RK, P. Koppenburg, M. Merk, A. Pellegrino, N. Tuning, Phys.Rev.Lett 109 (2012)

- Rare decay in SM, **very sensitive** to scalar New Physics

A. Buras, Proc.Sci.BEAUTY (2011)

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.2 \pm 0.2) \times 10^{-9}$$

- Experimentally bounded

LHCb, Phys. Rev.Lett 108 (2012)

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{exp}} < 4.5 \times 10^{-9} \quad @ 95\% \text{ C.L.}$$

Probing New Physics in $B_s \rightarrow \mu^+ \mu^-$

K. Bruyn, R. Fleischer, RK, P. Koppenburg, M. Merk, A. Pellegrino, N. Tuning, Phys.Rev.Lett 109 (2012)

- Rare decay in SM, **very sensitive** to scalar New Physics

A. Buras, Proc.Sci.BEAUTY (2011)

$$\text{BR}(B_s \rightarrow \mu^- \mu^-)_{\text{SM}} \stackrel{\Delta\Gamma_S \neq 0}{=} (3.5 \pm 0.2) \times 10^{-9}$$

- Experimentally bounded

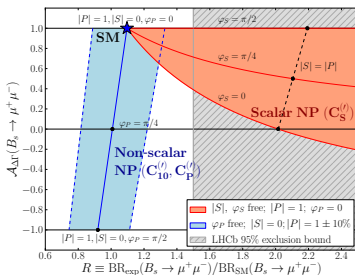
LHCb, Phys. Rev.Lett 108 (2012)

$$\text{BR}(B_s \rightarrow \mu^- \mu^-)_{\text{exp}} < 4.5 \times 10^{-9} \quad @ 95\% \text{ C.L.}$$

- Untagged observable:

$$\tau_{\mu^+ \mu^-} / \mathcal{A}_{\Delta\Gamma}^{\mu^+ \mu^-}$$

experimentally
feasible **probe** of NP



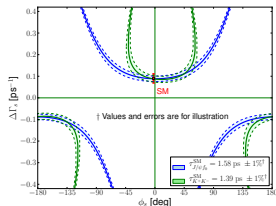
Summary

- CP observables \rightarrow SM predictions

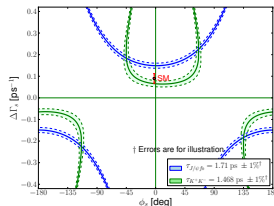
Disentangle **New Physics**
from **SM Hadronic Physics**

- Probe B_s mixing phase with **untagged** analysis:

Pair of CP odd and even **effective lifetimes**

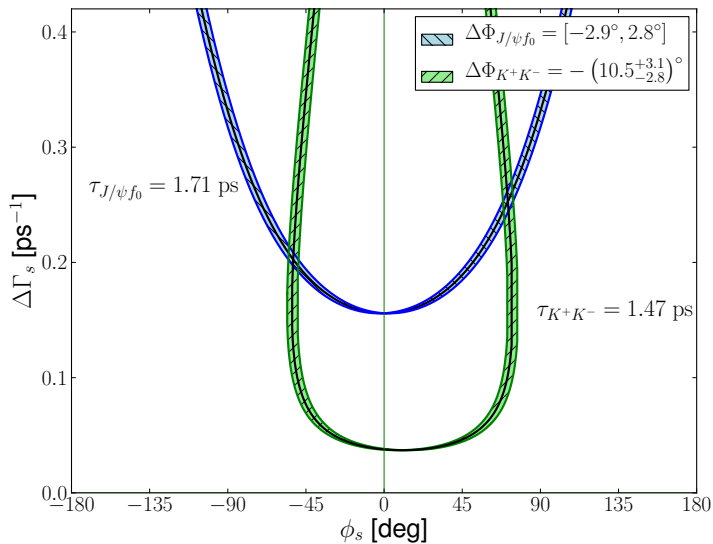


Summer
2013 ??



Backup

Hadronic uncertainties



Effective Lifetime

$$\tau = \frac{\tau_{B_s}}{1 - y_s^2} \left(\frac{1 + 2 \mathcal{A}_{\Delta\Gamma} y_s + y_s^2}{1 + \mathcal{A}_{\Delta\Gamma} y_s} \right)$$

$$\mathcal{A}_{\Delta\Gamma} = -\eta \sqrt{1 - C^2} \cos(\phi_s + \Delta\phi)$$

$$y_s^3 + \left(\frac{\tau_{B_s} - \tau}{\tau \mathcal{A}_{\Delta\Gamma}} \right) y_s^2 + \left(\frac{2\tau_{B_s} - \tau}{\tau} \right) y_s + \left(\frac{\tau_{B_s} + \tau}{\tau \mathcal{A}_{\Delta\Gamma}} \right) = 0$$

Notation

The CP asymmetry:

$$\frac{\Gamma(B_s(t) \rightarrow f) - \Gamma(\bar{B}_s(t) \rightarrow f)}{\Gamma(B_s(t) \rightarrow f) + \Gamma(\bar{B}_s(t) \rightarrow f)} = \frac{C \cos(\Delta M_s t) - S \sin(\Delta M_s t)}{\cosh(\Delta\Gamma_s t) + \mathcal{A}_{\Delta\Gamma} \sinh(\Delta\Gamma_s t)}$$

Observables for $\mathcal{CP}|f\rangle = \eta|f\rangle$:

$$\xi_f \equiv \frac{q}{p} \frac{A(\bar{B}_s^0 \rightarrow f)}{A(B_s^0 \rightarrow f)} = -\eta e^{-i\phi_s} \sqrt{\frac{1-C}{1+C}} e^{-i\Delta\phi}$$

$$\mathcal{A}_{\Delta\Gamma} - iS = \frac{2\xi_f}{1 + |\xi_f|^2} = \boxed{-\eta \sqrt{1 - C^2} e^{-i(\phi_s + \Delta\phi)}}$$

Tetraquarks

- diquark–antidiquark (colour) bound states

$$\sigma = [ud][\bar{u}\bar{d}]$$

$$\kappa = [su][\bar{u}\bar{d}]; [sd][\bar{u}\bar{d}] \quad (+c.d)$$

$$f_0 = \frac{[su][\bar{s}\bar{u}] + [sd][\bar{s}\bar{d}]}{\sqrt{2}}$$

$$a_0 = [su][\bar{s}\bar{d}]; \frac{[su][\bar{s}\bar{u}] - [sd][\bar{s}\bar{d}]}{\sqrt{2}}; [sd][\bar{s}\bar{u}]$$

diquark $\equiv [q_1 q_2]$, colour $\bar{\mathbf{3}}$, flavour $\bar{\mathbf{3}}$, $S = 0$

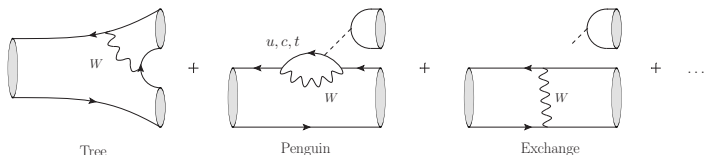
- Issues: $f_0 \rightarrow \pi\pi$ coupling too small, $a_0 \rightarrow \eta\pi$ too large.
- Solved by adding *instanton-induced effects*

A Theory of Scalar Mesons, G. 't Hooft, G. Isidori, A.D Polosa, V. Riquer,

(arXiv:0801.2288)

Decay Amplitudes: General Formalism

In reality:



$$\begin{aligned}
 \text{e.g. } A(B \rightarrow f) &= A_T + A_P^u + A_P^c + A_P^t + \dots \\
 &= |A_T| e^{i\delta_T} e^{i\varphi_T} + |A_P^u| e^{i\delta_u} e^{i\varphi_u} + |A_P^c| e^{i\delta_c} e^{i\varphi_c} + \dots \\
 &= |A_1| e^{i\delta_1} \left(e^{i\varphi_1} + e^{i\varphi_2} h e^{i\delta} \right)
 \end{aligned}$$

$$h e^{i\delta} \equiv \frac{A_2}{A_1} e^{i(\delta_2 - \delta_1)},$$

$$\xi = -\eta e^{-i\phi_s} \left[\frac{e^{-i\varphi_1} + e^{-i\varphi_2} h e^{i\delta}}{e^{i\varphi_1} + e^{i\varphi_2} h e^{i\delta}} \right]$$

Untagged observable: General Formalism

$$\xi = -\eta e^{-i\phi_s} \left[\frac{e^{-i\varphi_1} + e^{-i\varphi_2} h e^{i\delta}}{e^{i\varphi_1} + e^{i\varphi_2} h e^{i\delta}} \right]$$

$$\frac{2\xi}{1 + |\xi|^2} = -\eta \sqrt{1 - C^2} e^{-i(\phi_s + \Delta\phi)}$$

$$C = \frac{2 h \sin \delta \sin(\varphi_1 - \varphi_2)}{1 + 2 h \cos \delta \cos(\varphi_1 - \varphi_2) + h^2}$$

$$\Delta\Phi = \arctan \left(\frac{\sin 2\varphi_1 + 2 h \cos \delta \sin(\varphi_1 + \varphi_2) + h^2 \sin 2\varphi_2}{\cos 2\varphi_1 + 2 h \cos \delta \cos(\varphi_1 + \varphi_2) + h^2 \cos 2\varphi_2} \right)$$

$$\mathcal{A}_{\Delta\Gamma} = -\eta \cos \phi_s \quad \rightarrow \quad \mathcal{A}_{\Delta\Gamma} = -\eta \sqrt{1 - C^2} \cos(\phi_s + \Delta\phi)$$

The Decay Width Difference

$$\begin{aligned}\Delta\Gamma_s &\equiv \Gamma_L - \Gamma_H \\ &\simeq 2|\Gamma_{12}| \cos(\Theta_M - \Theta_\Gamma)\end{aligned}$$

- No absorptive New Physics: *Grossman (hep-ph:9603244)*

$$y_s = \frac{\Delta\Gamma_s^{\text{Th}}}{2\Gamma_s} \cos \tilde{\phi}_s, \quad \tilde{\phi}_s = 0.22^\circ + \phi_s^{\text{NP}}$$

- Theoretical calculation: *Lenz & Nierste (1102.4274)*

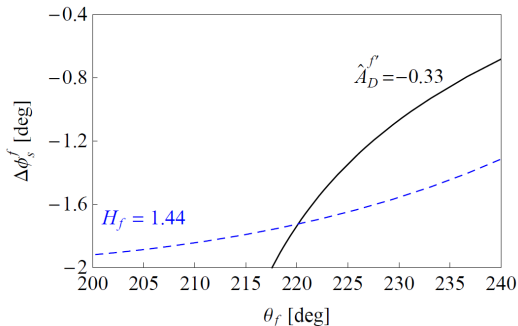
$$\frac{\Delta\Gamma_s^{\text{Th}}}{\Gamma_s} = 0.133 \pm 0.032$$

$B_s \rightarrow J/\psi\phi$ hadronic uncertainties

Measure : $\phi_s + \Delta\phi_{J/\psi\phi}^f$

- **Numerical example** compatible with $\Delta\phi_d$ analysis

S. Faller, R. Fleischer and T. Mannel, Phys.Rev. D79 (2009) 014005



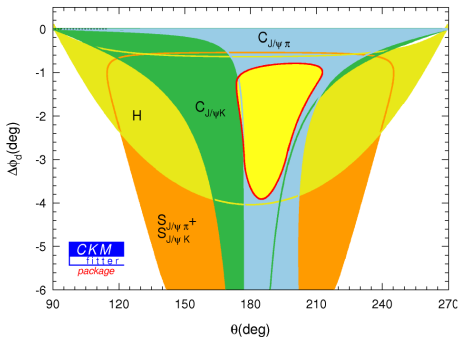
- Future control channels: $B_s \rightarrow J/\psi\bar{K}^{*0}$ and $B_d \rightarrow J/\psi\rho^0$

Hadronic uncertainty of $B_d^0-\bar{B}_d^0$ mixing

Measure : $2\beta + \Delta\phi_d$

Probe using $B_d \rightarrow J/\psi K_S$ and $B_d \rightarrow J/\psi \pi$

S. Faller, R. Fleischer, M. Jung, T. Mannel (arXiv:0809.0842)



See also: *Extracting gamma and Penguin Topologies through CP Violation in $B_s^0 \rightarrow J/\psi K_S$, K. De Bruyn, R. Fleischer and P. Koppenburg (arXiv:1010.0089)*